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DYNAMIC UNBALANCE DETERMINATION OF SUBMUNITION BOMBLETS.(U)
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(Supersedes IMR No. 593)

DYNAMIC UNBALANCE DETERMINATION OF
SUBMUNITION BOMBLETS

Clarence C. Bush
Charles J. Nietubicz

May 1979

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US ARMY ARMAMENT RESEARCH AND DEVELOPMENT COMMAND
BALLISTIC RESEARCH LABORATORY
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20. ABSTRACT (Continue on reverse side if necessary and identify by block number) (1cb) An experimental program has been conducted to determine the dynamic unbalance of inert submunition grenades and bomblets. Dynamic unbalance influences the free flight spin-up of these spherical-shaped, vaned bomblets and may cause improper performance of the bomblet fusing process. These bomblets, of known balance characteristics, will be dispersed by missiles and subsequently recovered. An attempt will be made by others to correlate the ground pattern and the armed or non-armed condition of the individual fusing mechanisms with the degree of dynamic unbalance of each bomblet.		

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I. INTRODUCTION

The bomblet unbalance data supplied in this report were determined by the Aerodynamics Research Branch, LFD, BRL, for eighty-five XM74 grenades and ninety-five BLU63 bomblets at the request of the Fluid Mechanics Branch, Applied Sciences Division, LCWSL, ARRADCOM, Dover, New Jersey.

A brief discussion is presented here as an aid to understanding the tabulated data, the methods for obtaining the data, and the accuracy of those determinations.

Measurements of axial and transverse moments of inertia, center of gravity locations, weights and polar diameters were supplied by the Fluid Mechanics Branch for use, in conjunction with the BRL measured mass unbalances, in the computation of the angle of unbalance of each bomblet (the angle formed by the geometric spin axis and the dynamic axis).

II. DATA ACQUISITION

Both types of bomblets have identical exterior size and shape, within manufacturing tolerances. Thus, a single fixture and model-holding adapter could be used during the unbalance measurements. The canister type adapter, shown in Figure 1, was designed and fabricated at the BRL. The adapter made use of a contoured inner surface, formed by a plastic molding process, to provide reproducibility of model positioning and the alignment of the model spin about its geometric axis.

Dynamic unbalance measurements were made on the empty fixture prior to the model's being installed; then these tare values were vectorially subtracted from the balancing measurements made with the bomblets in the fixture. Balancing data are given in gram-inches at two preselected measurement stations. The left measurement plane was established at the left end of the canister and the right measurement plane at the right end of the canister (refer to Figures 1 and 2).

A Balance Technology, Inc., Model D-75PS dynamic balancing machine was used for measuring the bomblet unbalances. This machine is specified as being capable of detecting peak-to-peak vibrations of .000025 inch for standard operation; a peak-to-peak displacement of .000025 inch represents a measurement of 0.1135 gram-inch (.004 ounce-inch) on a ten pound rotating mass. (The weight of the complete rotating assembly, including bomblet, used in these unbalance measurements was approximately five pounds. Thus, without consideration for the cantilever arrangement and unusually close-coupled measurement planes, the machine was capable of resolving unbalances of approximately 0.05 gram-inch during these bomblet unbalance measurements.)

obtain values for the products of inertia in that system. From the resulting inertia tensor, we could compute the three real eigenvalues I_1, I_2, I_3 and the directions of the three eigenvectors. Then in a coordinate system X_1, X_2, X_3 whose axes have the directions of these eigenvectors, the products of inertia vanish and the principal moments of inertia are I_1, I_2, I_3 . The angle of unbalance α is, then, the angle between the x and X_1 axes.

For lack of time, we performed an eigenanalysis only on a representative set of grenades and bomblets (Table I, column 14). Approximate values of α from Equation (1), however, were obtained for all the grenades and bomblets (Table I, column 13). For each eigenanalysis value of α , we computed a correction factor

$$\Delta = \alpha_e - \alpha_a \quad (2)$$

where subscript "e" denotes an exact (eigenanalysis) value and subscript "a" denotes the approximate value from Equation (1). Figure 3 is a plot of Δ versus α_a up to 34 degrees; the curve shown is a fairing through the plotted points. From this faired curve, we read a Δ value for each grenade and bomblet omitted from the eigenanalysis (Table I, column 15). Finally, we obtained corrected values of the angle of unbalance (Table I, column 16) by the relation

$$\alpha = \alpha_a + \Delta \quad (3)$$

IV. EXPERIMENTAL RESULTS

Table I presents the unbalance measurements made by BRL, the physical data supplied by the Fluid Mechanics Branch, the computed center of gravity offset, and the computed angle of unbalance for all 180 bomblets. The individual bomblets are identified by the Fluid Mechanics Branch code number listed in the initial column. These final results are summarized in histogram form in Figures 4 and 5.

V. DISCUSSION OF POSSIBLE ERROR

On page 8 it was indicated that the individual unbalances at the two planes of measurement were reproducible to within 0.3 gram-inch and their related angles to within ± 8 degrees. The accuracy of these values depends on the fixture calibrations. When a four gram mass of modeling clay was attached to the bomblet canister at the left measurement plane, a 3.75 gram dynamic unbalance resulted at the left plane indicator, and when a four gram mass of clay was added to the canister at the right measurement plane, a 3.95 gram dynamic unbalance resulted

at the right plane indicator. The precision fixture for unbalance calibrations was not used for this experiment because it does not represent a good replication of the actual geometry. As was expected, these results are only qualitative but do determine the location of the decimal point in the unbalance indicators.

For four independently repeated measurements on "control" grenade PA90A, the final angle of unbalance ranged from 7.1 to 8.2 degrees. This implies a $\pm 7.8\%$ range of measurement error from the mean measured value. Eleven independent balance measurements on "control" bomblet PA671 indicated from 8.8 to 11.0 degrees for the final angle of unbalance and that result equates to a $\pm 11.1\%$ range of measurement error from the mean measured value.

It is difficult to analyze the total possible error inherent in the complete measurement and computation procedure. In view of this difficulty, the Fluid Mechanics Branch, ASD, requested from LFD an alternative procedure for error investigation. This procedure employed trial computations with a 1% deviation in the input parameters to determine their individual effect on the final angles of unbalance. The result of this exercise determined the relative importance of each parameter in the final result. These data, presented in Table II, show that utmost accuracy is required in the moment of inertia measurements.

VI. CONCLUSIONS

A. Repeated measurements of the angle of unbalance of XM74 grenades and BLU63 bomblets indicate that these measurements are routinely reproducible to approximately ± 1 degree when care is taken to avoid all possible errors from machine drift, etc. This value of ± 1 degree allows for the imperfect repeatability of the bomblet position in the holding fixture, but does not allow for measurement inaccuracies in such things as the bomblet moments of inertia, weight, diameter and C.G. distance. Also, it assumes absolute performance accuracy from the balancing machine and from the data reduction computations. The error possibilities in the input parameters can be expected to have a degrading effect on the overall measurement and computation accuracy. Therefore, the overall error possibility is larger than the ± 1 degree measurement reproducibility but is estimated to be less than ± 2 degrees.

B. An intentional 1% deviation in the moment of inertia input can result in deviations of ± 5 degrees or more in the computed angle of unbalance. This indicates a need for utmost precision in acquiring those measurements. The bomblet diameter, C.G. distance, and unbalance measurements are less critical, but can also produce significant error.

ACKNOWLEDGEMENTS

The authors are indebted to Dr. Andrew Mark for his capable aid in gaining an understanding of the problem and the procedures required, to William Beims and James Harmon for their assistance in making the unbalance measurements, and to Raymond Lehman and Donald Mylin for their aid in the data reduction.

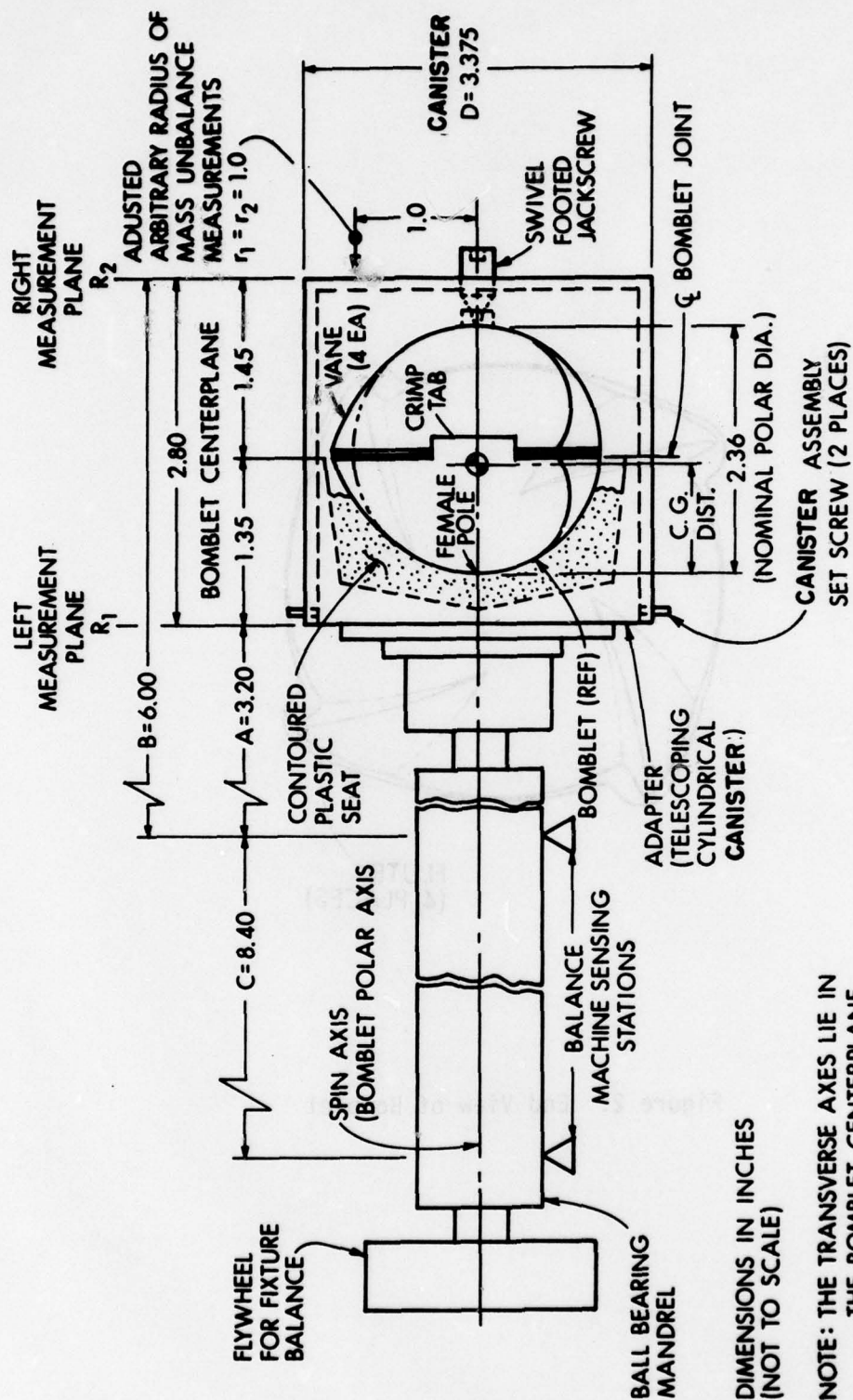


Figure 1. Balancing Geometry

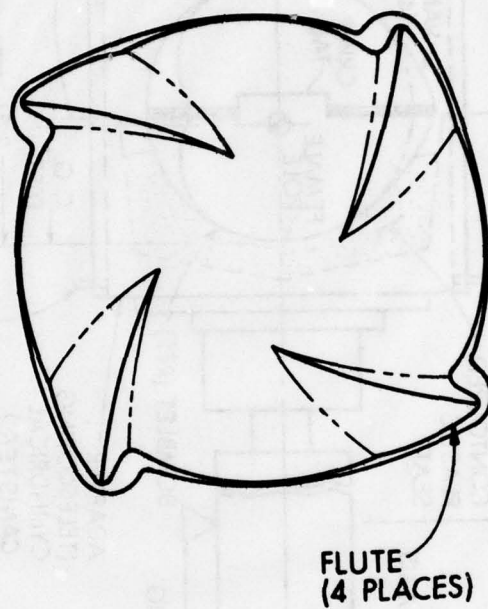


Figure 2. End View of Bomblet

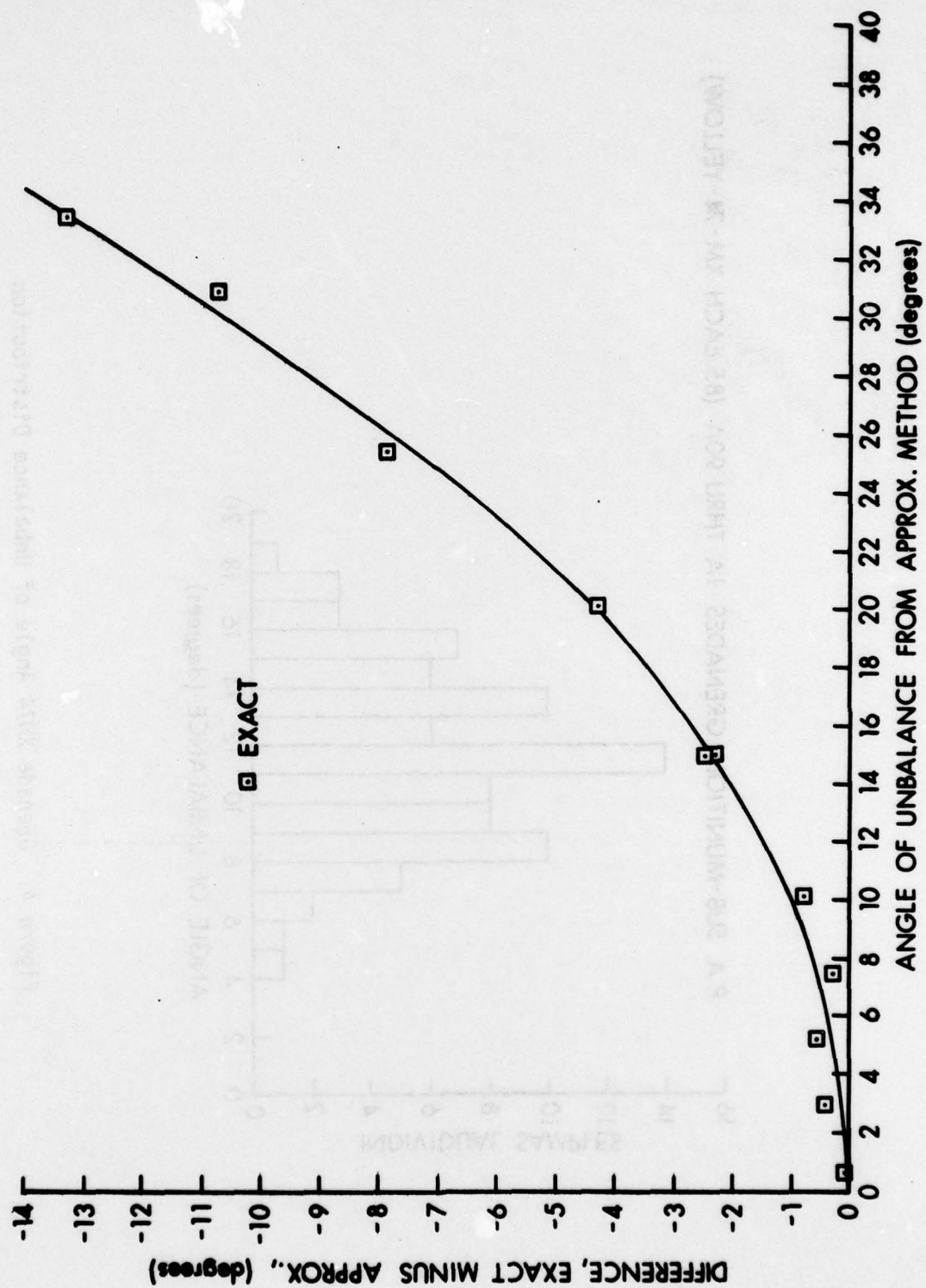


Figure 3. Procedure Correlation Graph

P.A. SUB-MUNITION GRENADES 1A THRU 90A (85 EACH XM-74-YELLOW)

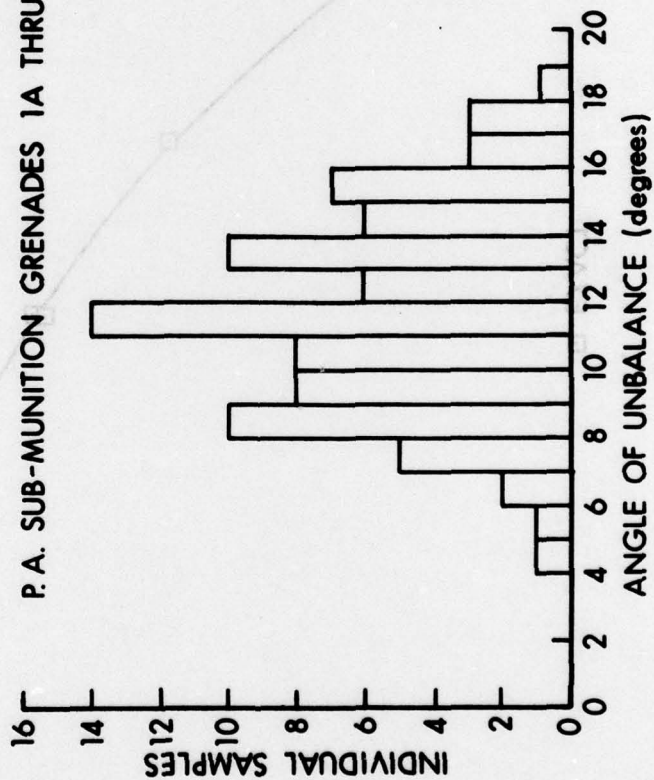


Figure 4. Grenade XM74 Angle of Unbalance Distribution

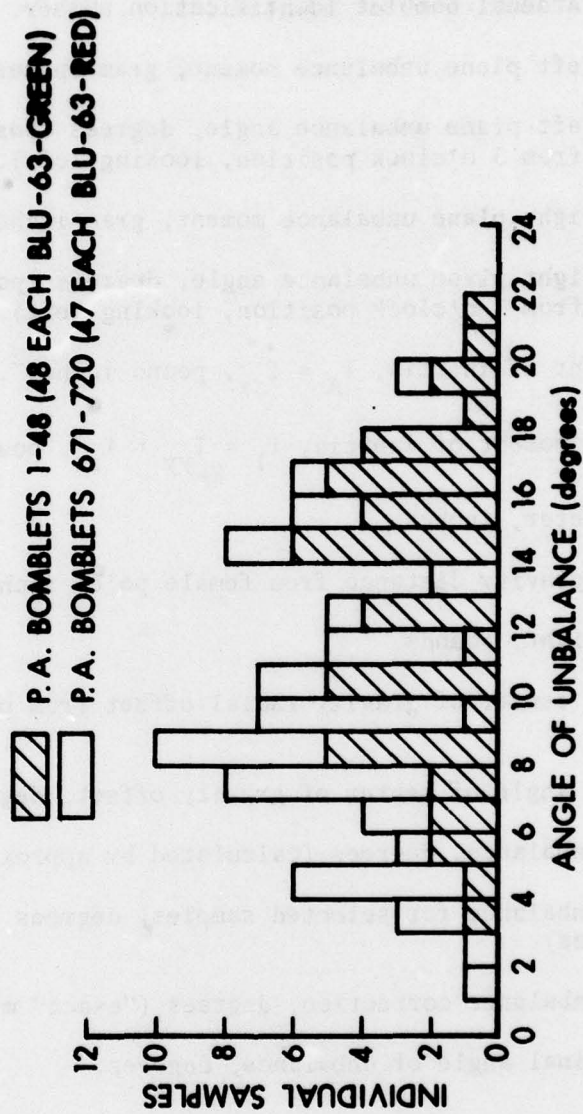


Figure 5. Bomblet BLU 63 Angle of Unbalance Distribution

Table I. Experimental Results

Column Headings for Table I.

1. Picatinny Arsenal bomblet identification number.
2. Measured left plane unbalance moment, gram-inches.
3. Measured left plane unbalance angle, degrees (positive, counter-clockwise from 3 o'clock position, looking left).
4. Measured right plane unbalance moment, gram-inches.
5. Measured right plane unbalance angle, degrees (positive, counter-clockwise from 3 o'clock position, looking left).
6. Axial moment of inertia, $I_A = I_{xx}$, pound inches².
7. Transverse moment of inertia, $I_T = I_{yy} = I_{zz}$, pound inches².
8. Polar diameter, inches.
9. Center of gravity distance from female pole, inches.
10. Bomblet weight, pounds.
11. Calculated center of gravity radial offset from polar axis, inches.
12. Calculated angle of center of gravity offset, degrees.
13. Angle of unbalance, degrees (calculated by approximate method).
14. Angle of unbalance for selected samples, degrees (calculated by exact method).
15. Angle of unbalance correction, degrees ("exact" minus approximate).
16. Adjusted final angle of unbalance, degrees.

Table I. Continued

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
FT	.0760	36.0	1.0200	290.0	.951	.917	2.350	1.195	1.255	.0031	29.0	8.91				8.16
1A	.2465	351.5	2.5245	305.0	.961	.925	2.347	1.179	1.270	.0111	104.4	19.46				15.46
2A	2.2780	7.5	5.6950	326.0	.974	.938	2.349	1.185	1.283	.0079	90.2	16.70				13.85
3A	1.4790	13.0	4.4080	335.0	.970	.933	2.349	1.180	1.281	.0041	59.9	8.65				7.85
4A	1.0112	11.5	2.7115	329.5	.953	.916	2.346	1.178	1.259	.0078	117.9	13.65				11.70
5A	1.9635	15.5	4.3520	316.0	.961	.920	2.350	1.185	1.264	.0094	96.7	11.88				10.68
FT	.7820	40.0	.9775	279.5	.964	.922	2.347	1.180	1.269	.0068	109.0	10.51				9.41
6A	2.0995	13.0	4.3690	337.5	.961	.922	2.347	1.179	1.263	.0086	90.7	13.41				11.61
7A	1.5640	22.5	3.6465	328.5	.971	.934	2.347	1.180	1.276	.0090	100.6	13.67				11.77
8A	1.7935	15.5	4.1310	344.5	.971	.934	2.347	1.179	1.280	.0079	84.5	8.96				8.16
9A	1.6575	357.5	4.8450	310.5	.968	.928	2.346	1.173	1.273	.0101	80.1	17.97				14.62
10A	2.1250	15.0	3.2725	352.5	.970	.930	2.350	1.190	1.274	.0104	93.6	18.59				14.99
FT	.8500	38.0	.9350	287.0	.961	.926	2.347	1.179	1.269	.0074	102.0	15.88				13.23
11A	1.6745	359.5	5.2700	335.5	.964	.927	2.349	1.174	1.271	.0053	105.9	7.89				7.29
12A	1.6575	19.0	3.6125	311.0	.965	.927	2.349	1.180	1.271	.0072	88.3	13.48				11.68
13A	1.5555	28.5	3.8845	349.5	.962	.924	2.349	1.180	1.268	.0063	118.5	10.90				9.65
14A	1.5385	6.5	3.0600	307.0	.971	.933	2.349	1.180	1.278	.0096	104.9	15.82				13.22
15A	1.3770	10.0	4.0375	329.0	.965	.930	2.352	1.176	1.273	.0101	87.8	18.67				15.02
FT	.8585	41.0	.9605	279.5	.973	.930	2.347	1.184	1.284	.0082	91.5	12.24				10.74
16A	1.6575	19.0	3.6125	311.0	.969	.933	2.353	1.181	1.277	.0079	92.7	10.36				9.36
17A	2.0995	19.0	4.7600	335.0	.962	.926	2.349	1.180	1.269	.0058	81.7	6.81				6.36
18A	1.9210	8.0	4.9300	339.0	.984	.945	2.351	1.185	1.301	.0107	96.6	17.16				14.11
19A	1.8020	7.0	4.1480	329.5	.968	.928	2.348	1.179	1.274	.0072	79.9	12.93				11.23
20A	1.9550	7.0	3.7825	329.0	.963	.920	2.351	1.171	1.263	.0090	99.9	15.18				12.78
FT	.8500	37.5	1.0115	281.0	.962	.925	2.351	1.181	1.268	.0103	105.8	16.67				13.82
21A	1.7850	14.0	2.6180	342.0	.969	.929	2.348	1.174	1.276	.0103	88.6	13.09				11.39
22A	2.0480	358.5	5.5675	321.0	.969	.930	2.349	1.190	1.277	.0117	82.3	19.01				15.21
23A	1.3770	8.0	3.9525	333.5	.965	.926	2.348	1.174	1.275	.0093	96.4	16.09				13.39
24A	1.6150	11.5	4.8790	326.0	.974	.938	2.350	1.180	1.284	.0071	108.7	10.65				9.55
25A	2.2780	18.0	4.9810	335.5	.966	.924	2.347	1.174	1.271	.0083	84.4	13.87				11.87
FT	.8585	43.0	.9945	293.5	.972	.937	2.351	1.178	1.268	.0104	86.6	19.74				15.64
26A	2.3460	8.0	4.7090	353.0	.958	.920	2.349	1.175	1.260	.0132	97.5	21.36				16.46
27A	2.0655	11.0	5.8650	340.5	.962	.923	2.350	1.180	1.265	.0077	101.8	9.78				8.81
28A	1.7340	10.5	3.9150	315.0	.961	.918	2.348	1.184	1.263	.0067	68.2	9.03				8.23
29A	1.8360	13.0	4.4965	340.5	.972	.931	2.347	1.186	1.260	.0071	91.4	8.10				7.50
30A	1.5300	13.0	4.4965	340.5	.968	.926	2.347	1.179	1.269	.0066	90.3	8.50				7.75
FT	.8585	47.0	1.1050	298.5	.956	.912	2.347	1.174	1.257	.0098	99.9	13.54				11.74
31A	1.8530	6.5	5.5250	337.5	.972	.937	2.351	1.178	1.260	.0104	86.6	19.74				15.64
32A	2.1080	346.0	6.8000	310.0	.962	.923	2.350	1.180	1.265	.0077	101.8	9.78				8.81
33A	1.7935	5.5	4.2075	316.5	.961	.918	2.348	1.184	1.263	.0067	68.2	9.03				8.23
34A	1.4535	1.5	3.6295	340.5	.972	.931	2.347	1.186	1.260	.0071	91.4	8.10				7.50
FT	.8415	51.0	1.0285	304.0	.968	.926	2.347	1.179	1.269	.0066	90.3	8.50				7.75
35A	1.4960	359.0	3.9100	318.0	.956	.912	2.347	1.174	1.257	.0098	99.9	13.54				11.74
36A	1.1135	353.5	3.8590	305.5	.972	.937	2.351	1.178	1.260	.0104	86.6	19.74				15.64
37A	1.7340	5.5	5.2700	321.0	.962	.923	2.350	1.180	1.265	.0077	101.8	9.78				8.81
38A	1.9890	.0	4.9980	327.0	.961	.918	2.348	1.184	1.263	.0067	68.2	9.03				8.23
39A	1.9890	357.0	5.1340	330.0	.978	.939	2.347	1.181	1.269	.0100	87.4	13.83				11.33
40A	.7565	46.0	.9265	296.0	.967	.927	2.348	1.179	1.275	.0110	93.5	16.20				13.50
FT	1.9550	357.0	5.6100	325.5	.980	.941	2.347	1.181	1.293	.0105	103.9	21.29				16.49
41A	1.5640	7.0	5.9500	320.0	.968	.929	2.348	1.174	1.275	.0062	99.0	11.01				9.81
42A	1.4110	358.5	3.7740	315.0	.971	.929	2.345	1.167	1.283	.0090	83.1	14.71				12.51
43A	1.4110	358.5	3.7740	315.0	.965	.924	2.345	1.175	1.271	.0097	103.8	14.89				12.44
44A	1.8105	8.5	5.1170	324.0	.967	.926	2.347	1.179	1.271	.0121	108.2	25.40				17.56
45A	.8415	32.0	.8925	271.0	.964	.922	2.345	1.183	1.269	.0123	91.4	19.26				15.36
46A	2.1505	358.5	5.9500	331.0												

Table I. Continued

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
49A		1.8445	16.0	4.8875	322.0	.968	.924	2.346	1.181	1.273	.0094	107.9	14.89		-2.30	12.59
50A		1.8870	353.0	5.2700	325.5	.962	.926	2.348	1.172	1.269	.0107	86.5	19.68		-4.05	15.63
51A		1.9465	24.0	3.3660	326.5	.967	.931	2.351	1.179	1.274	.0068	117.1	11.53		-2.30	9.23
FT		.8670	44.0	1.0370	298.0	.967	.927	2.351	1.181	1.272	.0091	87.4	16.95		-3.00	13.95
52A		1.5385	13.0	5.1000	330.0	.969	.933	2.351	1.173	1.276	.0074	99.8	9.39		-.00	8.59
53A		2.0400	18.0	3.7315	335.0	.971	.933	2.350	1.173	1.278	.0068	89.8	6.88		-.45	6.43
54A		1.9040	6.5	3.4510	331.0	.965	.923	2.344	1.185	1.274	.0060	75.6	9.83		-.00	8.23
55A		1.2920	9.0	3.5020	334.0	.974	.933	2.347	1.174	1.282	.0050	93.6	8.14		-.60	7.54
56A		1.3005	23.5	3.1110	332.5	.970	.939	2.347	1.179	1.290	.0106	102.5	18.06		-3.40	14.66
FT		.7400	32.5	.8670	267.0	.979	.939	2.347	1.179	1.290	.0106	102.5	18.06		-3.40	14.66
57A		1.9720	7.5	5.2275	329.0	.979	.939	2.349	1.180	1.291	.0085	121.0	16.62		-2.85	13.77
58A		1.6830	25.5	4.4880	330.0	.971	.931	2.346	1.181	1.278	.0089	103.8	12.65		-1.55	11.10
59A		1.9635	11.0	4.2330	329.0	.971	.931	2.346	1.181	1.278	.0089	103.8	12.65		-1.55	11.10
60A		2.0060	14.5	4.2160	334.0	.962	.919	2.349	1.175	1.264	.0091	103.8	12.01		-1.40	10.61
61A		1.5470	6.0	4.1650	332.5	.971	.934	2.356	1.173	1.280	.0083	91.4	15.25		-2.40	12.85
FT		.8075	34.5	.8840	270.0	.966	.924	2.347	1.174	1.271	.0098	102.1	11.46		-1.30	10.16
62A		2.3290	5.5	4.4540	324.5	.958	.919	2.346	1.176	1.265	.0096	99.5	20.98		-4.75	16.23
63A		1.5130	22.5	4.8705	348.0	.962	.926	2.345	1.171	1.274	.0115	102.0	17.84		-3.35	14.49
64A		2.5840	15.5	5.1000	341.0	.962	.926	2.345	1.171	1.274	.0115	102.0	17.84		-3.35	14.49
65A		2.0315	4.5	5.0150	326.0	.979	.940	2.348	1.177	1.280	.0102	99.5	16.45		-2.80	13.65
66A		1.7255	14.0	5.3550	334.0	.975	.934	2.347	1.174	1.288	.0103	102.2	20.02	15.64	.00	15.64
FT		.7905	34.0	.9435	270.0	.971	.934	2.352	1.184	1.276	.0121	89.8	25.28		-7.25	18.03
67A		1.8615	359.0	6.1200	330.5	.957	.917	2.346	1.171	1.259	.0037	74.3	5.50		-.30	5.20
68A		1.2750	22.0	1.5130	350.0	.962	.920	2.345	1.170	1.263	.0110	106.0	15.68		-2.55	13.13
69A		2.3630	15.5	5.1000	335.0	.962	.920	2.345	1.170	1.263	.0110	106.0	15.68		-2.55	13.13
70A		2.0230	33.0	3.4765	355.0	.981	.944	2.346	1.176	1.300	.0080	106.3	12.71		-1.65	11.06
72A		2.0910	19.5	4.0970	340.0	.967	.923	2.347	1.181	1.271	.0090	103.2	11.50		-1.35	10.15
FT		.8160	36.5	.9350	266.5	.962	.920	2.348	1.181	1.264	.0069	117.3	18.04		-1.00	9.04
73A		1.9210	27.5	3.3490	328.0	.961	.926	2.349	1.175	1.268	.0082	108.9	12.70		-1.60	11.10
76A		1.8955	5.5	3.9610	319.0	.977	.937	2.348	1.175	1.289	.0094	85.5	13.21		-1.80	11.41
77A		2.1335	15.0	3.9950	355.5	.973	.938	2.349	1.170	1.286	.0061	87.8	12.47		-1.50	10.97
78A		1.3260	12.5	3.2300	329.0	.973	.938	2.349	1.170	1.286	.0061	87.8	12.47		-1.50	10.97
79A		1.6405	349.0	5.1000	331.0	.954	.914	2.342	1.179	1.257	.0104	73.2	18.03		-3.40	14.63
FT		.8075	34.5	.9520	269.0	.970	.935	2.352	1.184	1.278	.0109	89.4	24.70		-6.80	17.90
80A		1.7000	.0	5.4825	338.0	.968	.932	2.349	1.180	1.277	.0122	96.9	24.42		-6.70	17.72
81A		2.1335	6.5	5.9500	334.0	.963	.922	2.345	1.168	1.264	.0073	111.7	11.77		-1.35	10.42
82A		1.7170	20.0	3.7230	326.0	.970	.929	2.348	1.182	1.275	.0095	114.7	14.92		-2.30	12.62
83A		2.0995	10.5	4.8450	315.0	.973	.936	2.348	1.182	1.275	.0095	114.7	14.92		-2.30	12.62
84A		1.8445	15.5	3.3490	325.0	.977	.936	2.350	1.180	1.283	.0068	105.4	9.00		-.80	8.20
FT		.8925	34.0	.9265	267.0	.964	.924	2.349	1.184	1.271	.0081	90.2	9.88		-.95	8.93
85A		1.9125	358.0	3.8165	321.0	.959	.917	2.345	1.180	1.265	.0040	96.3	4.44		-.20	4.24
86A		1.5300	24.5	1.7935	332.0	.969	.928	2.349	1.177	1.274	.0087	86.7	13.81		-1.90	11.91
87A		1.7765	6.5	4.2160	335.5	.959	.928	2.349	1.177	1.274	.0087	86.7	13.81		-1.90	11.91
88A		2.3035	13.0	3.8420	344.0	.970	.927	2.350	1.182	1.277	.0091	92.0	10.09		-1.00	9.09
89A		1.2410	2.0	2.7030	326.0	.955	.920	2.349	1.175	1.258	.0052	68.2	9.76		-.90	8.86
90A		1.6065	17.5	2.6435	353.0	.962	.920	2.346	1.173	1.266	.0061	79.2	9.00		-.80	8.20

Table I. Continued

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
FT																
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Table I. Concluded

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
FT																
671	.8495	40.0	.9520	288.0	.656	.632	2.356	1.170	.924	.0045	130.2	9.70			-.90	8.00
672	1.3605	23.0	2.4055	297.5	.655	.629	2.359	1.180	.922	.0046	90.9	8.21			-.70	7.51
673	1.2155	31.5	1.7850	346.0	.655	.626	2.360	1.180	.920	.0047	88.7	12.22			-1.50	10.72
674	1.6150	35.0	2.5585	10.0	.655	.628	2.366	1.180	.918	.0048	80.9	10.34			-1.05	9.29
675	1.6150	15.0	2.4905	343.5	.651	.625	2.359	1.170	.917	.0044	89.0	16.79			-2.95	13.44
676	1.4025	27.0	3.1705	352.0	.652	.625	2.359	1.170	.917	.0044	89.0	16.79			-2.75	13.47
677	1.4025	15.0	2.4565	1.0	.655	.631	2.361	1.180	.922	.0046	68.7	16.22			-1.80	11.52
678	1.1900	26.5	2.4565	1.0	.657	.633	2.357	1.179	.926	.0047	73.9	13.32			-.90	8.95
679	1.5555	51.0	1.4075	70.0	.657	.633	2.357	1.179	.926	.0047	73.9	13.32			-.90	8.95
680	1.4705	22.0	2.0825	352.5	.655	.631	2.358	1.179	.927	.0048	76.3	9.85			-.90	8.95
681	.8245	22.5	1.2495	335.0	.657	.634	2.350	1.179	.924	.0043	10.4	7.54			-.90	7.33
682	.8245	31.0	1.7000	291.0	.652	.626	2.350	1.170	.918	.0041	126.8	4.61			-.30	4.31
683	.9350	31.0	1.7000	291.0	.652	.626	2.350	1.170	.918	.0041	126.8	4.61			-.30	4.31
684	1.1500	23.0	3.2895	292.5	.652	.628	2.360	1.190	.918	.0043	136.1	17.12			-3.05	14.07
685	1.3365	22.0	3.1450	312.0	.651	.627	2.366	1.183	.917	.0046	119.6	14.74			-2.25	12.49
686	1.0540	23.5	1.6445	350.0	.653	.629	2.361	1.176	.919	.0046	55.3	11.06			-1.20	9.46
687	1.0150	41.0	2.1675	26.5	.656	.633	2.359	1.190	.925	.0043	85.1	12.95			-1.75	11.20
688	1.2495	39.0	2.8145	366.5	.649	.623	2.348	1.174	.914	.0032	147.0	7.97			-.70	7.27
FT																
689	.7820	37.0	.0670	280.5	.667	.646	2.366	1.183	.933	.0076	86.6	19.72			-4.05	15.67
690	1.3515	32.0	2.4820	10.0	.655	.629	2.369	1.175	.919	.0048	83.1	13.56			-1.45	11.71
691	1.2645	24.5	2.4225	353.5	.655	.629	2.369	1.175	.919	.0048	83.1	13.56			-1.45	11.71
692	1.1475	35.5	1.0285	359.0	.662	.640	2.365	1.183	.929	.0037	81.2	7.35			-.50	6.85
693	1.5385	15.5	3.8135	205.5	.655	.631	2.353	1.172	.921	.0040	.0	.00			.00	23.45
694	1.0795	24.5	2.4900	290.0	.660	.634	2.360	1.170	.926	.0044	141.6	10.98			-1.20	9.78
FT																
695	.9225	41.5	1.1850	290.0	.654	.631	2.360	1.182	.919	.0046	218.7	5.81			-.35	5.46
696	1.1305	33.5	1.2920	268.5	.659	.635	2.361	1.186	.926	.0040	.0	.00			.00	25.19
697	1.6235	24.5	5.0650	347.5	.654	.627	2.354	1.177	.920	.0046	320.8	4.66			-.25	4.41
698	1.1050	32.5	.0505	267.5	.654	.625	2.358	1.179	.916	.0049	112.5	2.90			.00	2.42
699	1.1390	41.0	1.3600	315.0	.651	.625	2.358	1.179	.916	.0049	112.5	2.90			.00	2.42
700	1.8275	28.0	5.1595	356.0	.655	.631	2.359	1.182	.923	.0040	.0	.00			.00	23.35
FT																
701	.0415	48.0	1.0540	304.0	.659	.635	2.353	1.172	.927	.0040	119.0	9.28			-.85	8.43
702	.8755	26.5	2.4140	289.0	.650	.624	2.356	1.178	.916	.0037	138.7	10.67			-1.10	9.57
703	.8500	51.5	1.0455	36.0	.650	.624	2.356	1.178	.916	.0037	138.7	10.67			-1.10	9.57
704	1.9965	33.5	2.5675	298.0	.664	.639	2.356	1.176	.929	.0039	142.1	10.09			.00	9.32
705	1.0285	26.5	.4080	27.0	.654	.629	2.353	1.182	.920	.0022	343.4	9.97			-1.00	8.97
706	1.2665	26.5	1.2920	341.0	.656	.630	2.365	1.183	.922	.0030	65.9	3.67			-.20	3.47
707	.7905	40.5	.6120	270.0	.660	.634	2.358	1.174	.927	.0029	30.6	7.61			-.55	7.06
708	1.2155	35.5	.5015	126.5	.661	.638	2.372	1.184	.927	.0041	112.5	9.73			-.90	8.83
709	1.0800	34.0	1.6660	329.0	.658	.633	2.367	1.184	.922	.0038	148.4	10.34			-1.00	9.34
710	1.3260	32.0	1.9380	292.0	.658	.633	2.367	1.184	.922	.0038	148.4	10.34			-1.00	9.34
711	1.7000	16.0	3.7825	349.0	.656	.630	2.362	1.179	.921	.0114	89.4	21.36			-4.95	16.41
712	1.7000	30.0	.7565	22.0	.655	.630	2.367	1.181	.921	.0040	78.2	4.91			-.25	4.66
713	.7565	40.5	.6290	272.5	.657	.632	2.357	1.181	.924	.0052	97.8	4.42			-.20	4.22
714	1.3430	45.0	1.2155	.0	.652	.626	2.351	1.168	.914	.0072	86.4	13.81			-1.90	11.91
715	1.3430	45.0	1.9550	44.0	.652	.626	2.351	1.168	.914	.0072	86.4	13.81			-1.90	11.91
716	1.3515	34.0	1.1730	315.5	.652	.625	2.356	1.183	.917	.0072	112.9	3.61			-.15	3.46
717	2.1675	25.5	4.6920	350.0	.656	.631	2.354	1.177	.921	.0143	105.3	29.63			-10.30	19.33
718	1.3770	39.0	.7395	334.5	.661	.635	2.352	1.174	.925	.0032	96.0	1.30			-.05	1.25
719	1.7000	30.0	2.9665	315.5	.653	.629	2.359	1.177	.919	.0076	131.9	17.80			-3.30	14.50
FT																
720	.9775	44.5	.8160	287.5	.657	.631	2.357	1.179	.921	.0064	77.9	7.75			-.60	7.15
721	1.7170	24.0	1.9890	354.5	.653	.626	2.360	1.188	.919	.0040	123.9	6.70			-.45	6.25
722	1.4450	31.5	1.9890	307.0	.654	.627	2.368	1.164	.918	.0042	63.2	8.49			-.70	7.79
723	1.2495	55.0	.6970	133.5	.654	.627	2.368	1.164	.918	.0042	63.2	8.49			-.70	7.79
724	1.6280	27.0	3.0050	16.5	.663	.636	2.368	1.182	.929	.0085	59.9	19.75			-4.10	15.65
725	1.2750	34.0	1.2835	340.0	.655	.630	2.357	1.181	.920	.0033	78.9	5.14			-.50	4.44
726	1.1730	20.5	2.7285	324.0	.655	.629	2.356	1.176	.922	.0062	80.6	12.29			-1.50	10.79

Table II. Effect of Input Deviations

Resulting Deviations in Angle of Unbalance

Trial Individual 1% Deviations (By Approximate-Type Method)	PA-26		PA-11		PA-3	
	(Low Residual Unbalance)		(Med. Residual Unbalance)		(High Residual Unbalance)	
	Deg.	%	Deg.	%	Deg.	%
Example Unbalance Condition (Degrees)	(5.43)		(12.11)		(23.31)	
A. 1% Deviation in Bomblet Weight	0	0	0	0	0	0
B. 1% Deviation in Bomblet Diameter	± .12	± 2.2	± .24	± 2.0	± .32	± 1.4
C. 1% Deviation in C.G. Distance	± .12	± 2.2	± .28	± 2.3	± .32	± 1.4
D. 1% Deviation in Axial Moment of Inertia (I_{xx})	± 1.14	± 21.0	± 2.64	± 21.8	± 5.82	± 25.0
E. 1% Deviation in Transverse Moment of Inertia (I_{yy})	± 1.87	± 34.5	± 4.58	± 37.8	± 15.80	± 67.8
F. 1% Deviation in Transverse Moment of Inertia (I_{zz})	± 1.87	± 34.5	± 4.58	± 37.8	± 15.80	± 67.8
G. 1% Deviation in Left Plane Unbalance	± .09	± 1.7	± .13	± 1.1	± .12	± .5
H. 1% Deviation in Left Plane Unbalance Angle	± .23	± 4.2	± .10	± .8	± .05	± .2
I. 1% Deviation in Right Plane Unbalance	± .46	± 8.5	± .25	± 2.1	± .34	± 1.5
J. 1% Deviation in Right Plane Unbalance Angle	± .11	± 2.0	± .74	± 6.1	± .05	± .2

NOTE: A 1% deviation of items H and J is taken as $360/100 = 3.6$ degrees.

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1. Donald T. Greenwood, Principles of Dynamics, Prentice-Hall, 1965.
2. Material Test Procedure 4-2-801, APG, MD, Projectile Unbalance, 29 September 1965.

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